

TMDs studies with RF-separated beams



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TMDs /beams

- TMDs of various (unpolarized) hadrons
- $-----//-----$ of valence antiquarks
- Universality of TMDs of (polarized) target
- Flavour separation



TMDs vs GPDs

- Theoretically: Sivers $f(x) \sim L(x)E(x)$ –
Lensing function
- $\Sigma \langle x E(x) \rangle = 0 \rightarrow$ Ji's SR's
(=Equivalence principle: AGM=0;
Kobzarev, Okun'62)
- $\Sigma \langle x f(x) \rangle = 0$ –Burkardt SR
- Conjecture(OT'06): $\langle x f(x) \rangle \sim \langle x E(x) \rangle$
- $L(x)$??

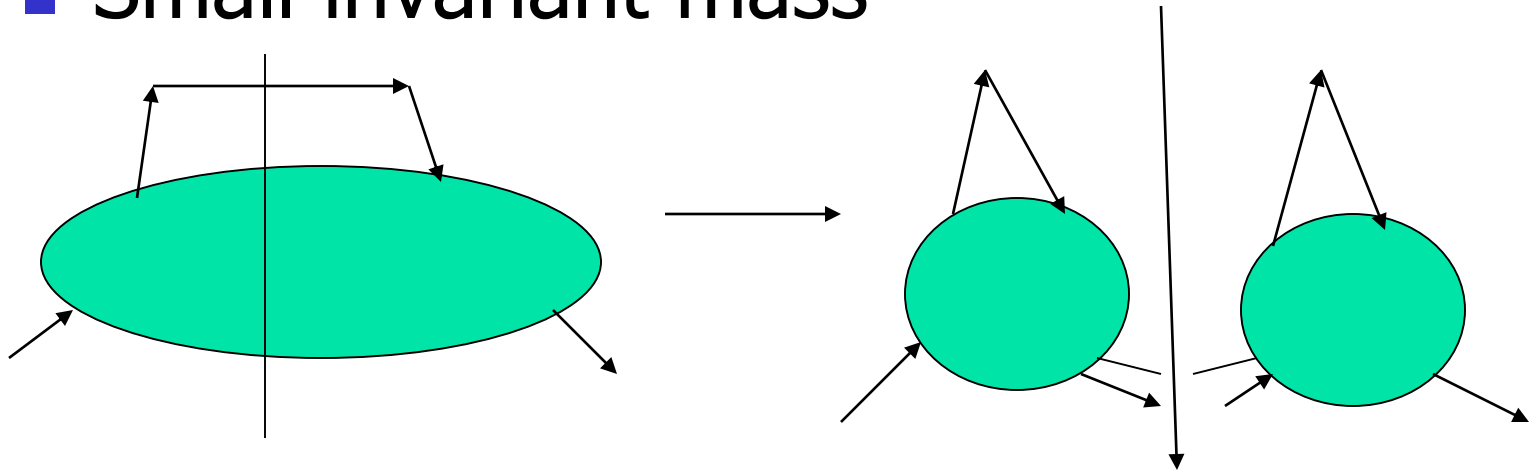


- TMDs vs FFs?

- Large x ?!

Exclusive limit : DIS and space-like (transitional and elastic) FFs

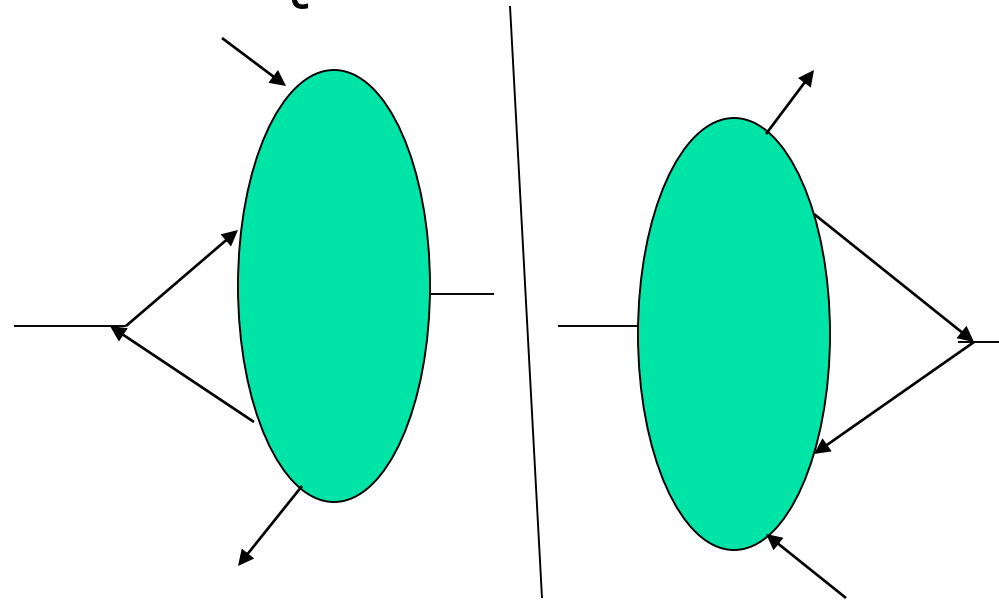
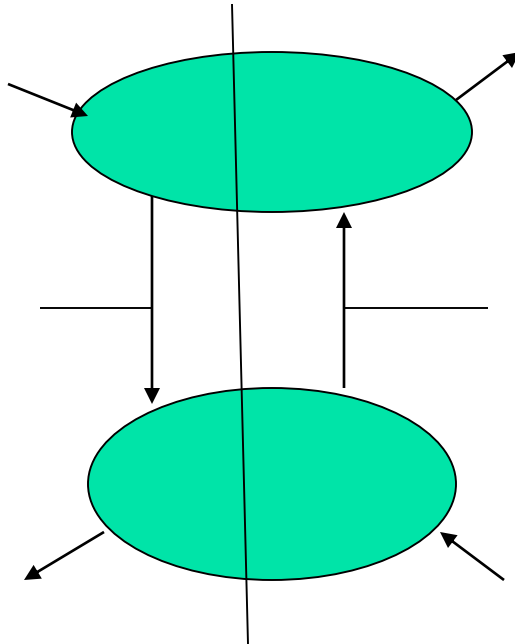
- Small invariant mass



- BG duality and DYW relation
- Relation between $x \rightarrow 1$ and large Q^2
- pdf $\sim (FF)^2$

Exclusive limit of DY and time-like FFs (OT'14)

- (Proton-antiproton) DY at small $s - Q^2$



$$(pdf)^2 \sim (\text{Dirac}) (FF)^2$$

- Other beams – baryon number conservation – time-like transition FFs

Comparing space-like and time-like FFs

- “Duality intervals” - from mass to x-space
- DIS: $(P+q)^2 = (P_f + \delta P_{DIS})^2 = (M + \mu_{DIS})^2$ $\mu_{DIS} \sim$ pion related scale
- Deviation of $x_B (\equiv 1 - \delta_{DIS})$ from 1
$$\delta_{DIS} \sim 2M\mu_{DIS}/Q^2.$$
- DY: $(P_1 + P_2)^2 = (q + \delta P_{DY})^2$
- Deviation of $\tau = Q^2/s (\equiv 1 - \delta_{DY})$ from 1
$$\delta_{DY} \sim 2\mu_{DY}/Q$$



DR: FFs from duality intervals

- DIS: $F_{SL}^2 \sim \int_0^{\delta_{DIS}} d\bar{x} f(\bar{x}) \quad x = 1 - \bar{x}$

- DY: $F_{TL}^2 \sim \int_0^{\delta_{DY}} d\bar{x}_1 d\bar{x}_2 f(\bar{x}_1) f(\bar{x}_2) \delta(\delta_{DY} - \bar{x}_1 - \bar{x}_2)$

- Proton-antiproton DY –same parton distributions $f(\bar{x}) = C\bar{x}^a$

$$F_{SL}^2(Q^2) \sim \frac{C}{a+1} \left(\frac{2M\mu_{DIS}}{Q^2} \right)^{a+1} ; F_{TL}^2(Q^2) \sim \frac{C^2}{2(a+1)} \left(\frac{4\mu_{DY}^2}{Q^2} \right)^{a+1}$$

- Pion: $a=1$ ('effective' pdf) supported !



SL vs TL

- Same Q-dependence
- Normalization –defined by distribution scale (~ 5) and duality intervals
- Asymptotically coincide – scales close to QCDSR pion duality interval (rather than pion mass) similar (equal?!) for DIS and DY)!



Sivers function and formfactors

- Relation between Sivers function and AMM known on the level of matrix elements (Brodsky, Schmidt, Burkardt)
- Phase?
- Duality for observables?

BG/DYW type duality for DY SSA in exclusive limit

- Proton-antiproton DY – valence annihilation – analyticity - cross section is described by Dirac FF squared
- The SSA similar to Sivers one- due to interference of Dirac and Pauli FF's with a phase shift (Rekalo, Brodsky)
- Exclusive large energy limit; $x \rightarrow 1$:
 $f(x)/q(x) \rightarrow \text{Im } F_2/F_1(Q^2 \sim M^2(1-x))$
- Both directions – estimate of Sivers at large x and explanation of phases in FF's